Open Tests: Harvard Measurement Lab

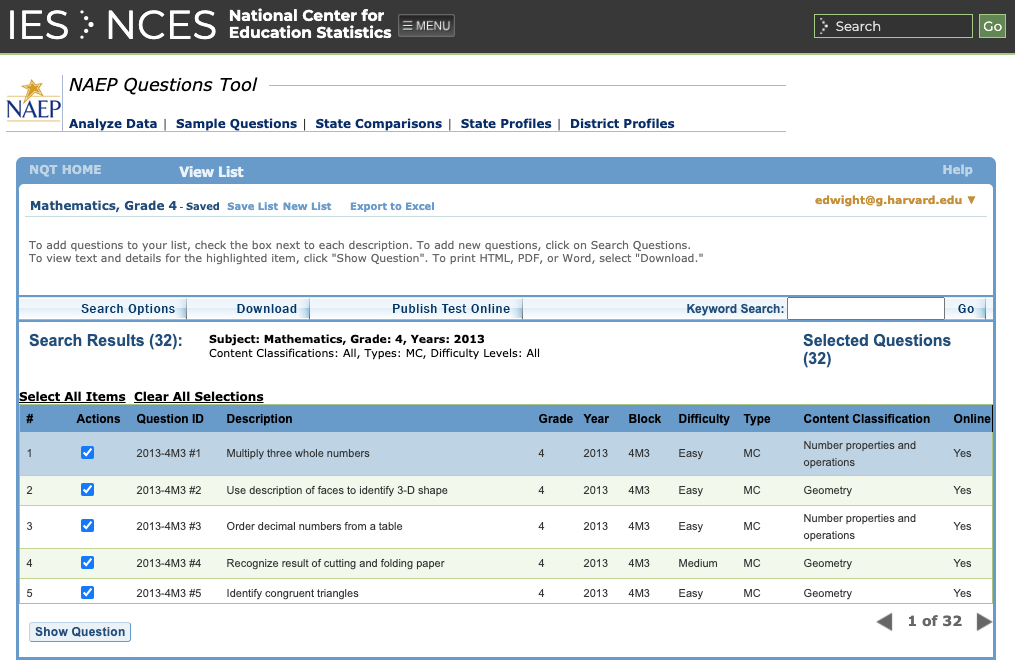
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In this tutorial we show how schools, districts, and states can create and score a test comprised of publicly available questions. As our example, we use released items from the 2013 administration of NAEP 4th Grade Math.

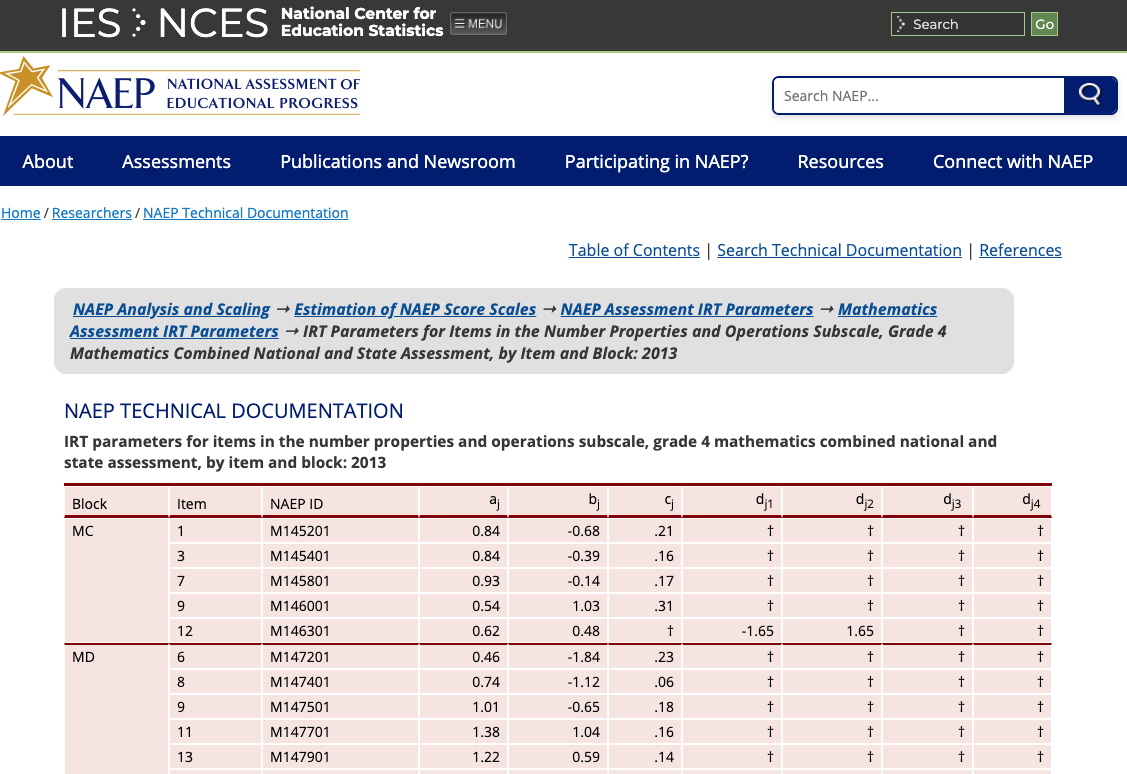
# Ingredients:

1. Released test questions (items) to create the test, like these:



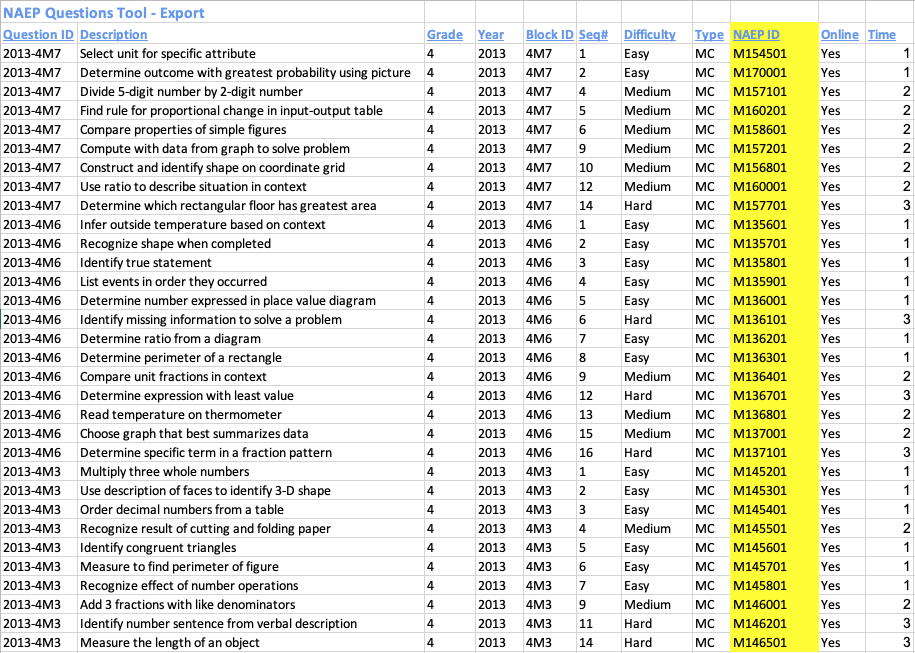
<https://nces.ed.gov/NationsReportCard/nqt/Search>

1. Released item IRT parameter estimates, like those found here: (Note that for NAEP, you will need to combine IRT parameters from each of the subscales to create an overall item pool)



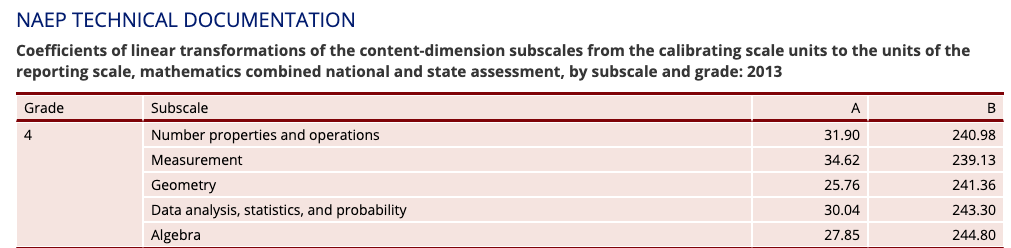
<https://nces.ed.gov/nationsreportcard/tdw/analysis/scaling_irt_math.aspx>

1. Common item numbers/identifiers that relate each question (item) to its parameters: (To get the IDs for questions from NAEP, using the NAEP Questions Tool to select multiple choice questions from your chosen year, click OK, then select all items, then “Export to Excel”)



<https://nces.ed.gov/NationsReportCard/nqt/Search#>

1. Student scores. For our tutorial, these can either be sum scores, or correct/incorrect responses for each of the test questions. (For NAEP items, you should consider exploring “Download…Test Kit” for paper administration or “Publish Test Online” for online administration once you’ve chosen your items in the NAEP Questions Tool.)
2. A table or equation that converts theta scores to reporting scale scores (and possibly also achievement levels), like this:



<https://nces.ed.gov/nationsreportcard/tdw/analysis/2013/trans_constants_math2013.aspx>

For NAEP, cut scores separating achievement level can be found here: <https://nces.ed.gov/nationsreportcard/mathematics/achieve.asp#grade4>

# Contents:

### Estimated Student Scale Scores from Sum Scores:

* Import 3PL IRT item parameters
* Import theta to scale score equation or table
* Import (or simulate) student response data
* Estimate student thetas using sum scores
* Convert estimated thetas to scale scores
* Produce table converting sum scores to scale scores, using Test Characteristic Curve information
* Export student ability data, including estimated thetas, scale scores, and achievement levels

### Appendix 1: Simulating Imprecision for Sum Score Theta Estimates

* Invert the Test Characteristic Curve to Produce Estimates of Standard Errors
* Produce table converting sum scores to scale scores, with empirical standard errors, using simulations

### Appendix 2: Scale Score Estimation Using Full-Pattern Scoring

* Estimate student ability using full-pattern scoring, (includes standard errors)
* Export student ability data, including estimated thetas, standard errors, scale scores, and achievement levels

### Appendix 3: Diagnostics

* Report Classical Test Theory statistics
* Plot Item Characteristic Curves and Test Characteristic Curve
* Plot Item Information Functions and Test Information Function

# Estimated Student Scale Scores from Sum Scores:

### Importing item parameters and scale scores

# Import selected items  
selected\_items <- read.csv("Selected\_Items.csv", skip = 1)  
  
# Pull out vector of NAEP IDs for selected items  
item\_IDs <- selected\_items$NAEP.ID  
  
# Import item parameter data  
item\_parameters\_raw <- read.csv("IRT\_Parameters.csv")   
  
# Subset the item parameters, keeping only those whose IDs are in item\_IDs  
item\_parameters\_selected <- subset(item\_parameters\_raw, item\_parameters\_raw$NAEP.ID %in% item\_IDs)  
  
# Drop some unnecessary rows  
item\_parameters <- item\_parameters\_selected %>% dplyr::select(NAEP.ID, aj, bj, cj, Subscale)  
  
# Turn this into the matrix form that irtoys expects  
my\_ip <- as.matrix(item\_parameters %>% dplyr::select(aj, bj, cj))   
  
# NAEP Technical Documentation shows that a normalizing constant D of 1.7 is used in their 3PL equations:  
# See here: https://nces.ed.gov/nationsreportcard/tdw/analysis/scaling\_models\_3pl.aspx  
# The R package irtoys uses a normalizing constant of 1, so we adjust all NAEP parameters accordingly  
D <- 1.7 # Change to D = 1 if none appears in your technical report  
# Divide "a" parameters by D to "undo" the normalizing constant and fit what the package irtoys expects  
my\_ip[,1] <- my\_ip[,1]/D  
  
# View first five rows  
my\_ip[1:5, ]

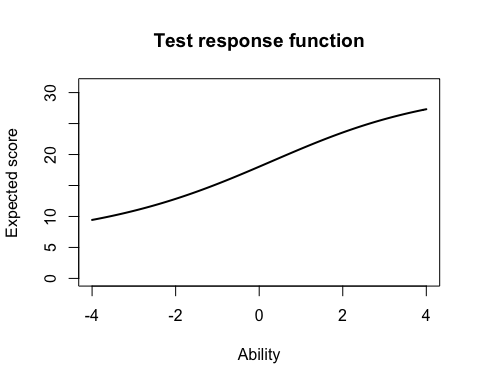
## aj bj cj  
## 1 0.4941176 -0.68 0.21  
## 2 0.4941176 -0.39 0.16  
## 3 0.5470588 -0.14 0.17  
## 4 0.3176471 1.03 0.31  
## 19 0.4411765 -0.62 0.39

# Import student responses (if using real data)  
  
  
# Import theta -> scale score equations  
scale\_scores\_raw <- read.csv("Scale\_Score\_Equations.csv")  
  
# These scale score equations for NAEP are separated by subscale. We offer two possible methods for combining these for an overall math equation. Select whichever makes the most sense for your situation.   
  
# Takes theta(s), returns scale score(s)  
# theta\_to\_scale\_score <- function(theta)  
# {  
# # Simplified version: just use the number properties and operations parameters  
# return(scale\_score = scale\_scores\_raw$A[1]\*theta + scale\_scores\_raw$B[1])  
# }  
  
# Takes theta(s), returns scale score(s)  
theta\_to\_scale\_score <- function(theta, weights = c(0.4, 0.2, 0.15, 0.1, 0.15))  
{  
 # Complex version: weighted average of each of the five subscale equations  
 # Default weights taken from here for 2013 grade 4 Math:   
 # https://nces.ed.gov/nationsreportcard/tdw/analysis/scaling\_determination\_composite.aspx  
 # Alternatively, user can provide weights customized to the actual distribution of questions used  
 A = weighted.mean(x = scale\_scores\_raw$A, w = weights)  
 B = weighted.mean(x = scale\_scores\_raw$B, w = weights)  
 return(scale\_score = A\*theta + B)  
}  
  
# If applicable, this function takes scale scores and returns achievement levels  
  
# Takes theta(s), returns scale score(s)  
scale\_score\_to\_achievement\_level <- function(scale\_scores, cutoffs = c(214, 249, 282))  
{  
 # Note that these cutscores can vary by grade, subject, and year  
 # Default cutoffs taken from here for 2013 grade 4 Math:   
 # https://nces.ed.gov/nationsreportcard/mathematics/achieve.asp#grade4  
 achievement\_levels <- rep("Below Basic", length(scale\_scores))   
 achievement\_levels[scale\_scores >= cutoffs[1]] <- "Basic"  
 achievement\_levels[scale\_scores >= cutoffs[2]] <- "Proficient"  
 achievement\_levels[scale\_scores >= cutoffs[3]] <- "Advanced"  
 return(achievement\_levels)  
}

### Scale Score Estimation Using Sum Scoring

“Invert” the TCC to get a map from sum scores to thetas:

# Plot Test Characteristic Curve (which underlies all of what follows)  
# Theta on x axis, predicted sum score on y axis  
plot(trf(my\_ip))



# Create a range of possible thetas  
thetas = seq(from = -5, to = 5, length.out = 100001)  
# Calculate the estimated sum score for each of these thetas   
all\_sum\_scores <- trf(my\_ip, x = thetas)  
  
# Simplifies the above possible sum scores (decimals) into possible whole number scores  
possible\_sum\_scores <- seq(from = ceiling(all\_sum\_scores$f[1]), to = floor(all\_sum\_scores$f[100000]), by = 1)  
  
# For each possible whole number score, find the associated theta that's the best match  
matching\_theta\_scores <- rep(NA, times = length(possible\_sum\_scores))  
for(i in 1:length(possible\_sum\_scores)) {matching\_theta\_scores[i] <- all\_sum\_scores$x[which.min(abs(all\_sum\_scores$f - possible\_sum\_scores[i]))]}  
  
# Produce a table with sum scores, thetas, scale scores, and achievement levels  
matching\_theta\_scores\_df <- as.data.frame(cbind(possible\_sum\_scores, matching\_theta\_scores))  
colnames(matching\_theta\_scores\_df) <- c("SumScore", "Theta")  
  
# Convert the thetas to scale scores and then achievement levels, using our custom functions above  
matching\_theta\_scores\_df$ScaleScore <- theta\_to\_scale\_score(matching\_theta\_scores\_df$Theta)  
matching\_theta\_scores\_df$AchievementLevel <- scale\_score\_to\_achievement\_level(matching\_theta\_scores\_df$ScaleScore)  
  
# Round the Scale Scores before reporting  
matching\_theta\_scores\_df$ScaleScore <- round(matching\_theta\_scores\_df$ScaleScore)  
  
# View table  
matching\_theta\_scores\_df

## SumScore Theta ScaleScore AchievementLevel  
## 1 9 -4.3668 107 Below Basic  
## 2 10 -3.5854 131 Below Basic  
## 3 11 -2.9490 151 Below Basic  
## 4 12 -2.4066 168 Below Basic  
## 5 13 -1.9287 182 Below Basic  
## 6 14 -1.4966 195 Below Basic  
## 7 15 -1.0976 208 Below Basic  
## 8 16 -0.7221 219 Basic  
## 9 17 -0.3630 230 Basic  
## 10 18 -0.0139 241 Basic  
## 11 19 0.3305 252 Proficient  
## 12 20 0.6756 262 Proficient  
## 13 21 1.0269 273 Proficient  
## 14 22 1.3905 284 Advanced  
## 15 23 1.7737 296 Advanced  
## 16 24 2.1861 309 Advanced  
## 17 25 2.6412 323 Advanced  
## 18 26 3.1596 339 Advanced  
## 19 27 3.7756 357 Advanced  
## 20 28 4.5549 381 Advanced

# Export table  
write.csv(matching\_theta\_scores\_df, file = "Estimated\_Scale\_Scores\_From\_Sum\_Scores.csv", row.names = F)

# Appendix 1: Simulating Imprecision for Sum Score Theta Estimates

How do we convey a sense of uncertainty with these sorts of score estimates?

Because students with “fixed” thetas can retake the test and score slightly differently each time, we simulate this below to create an empirical range of possible scale scores for each student sum score.

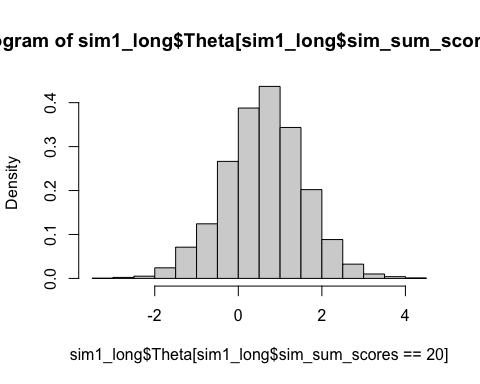
# Create a sequence of possible thetas, equally spaced  
sim\_thetas <- seq(from = -5, to = 5, length.out = 1001)  
  
# Replicate each of the possible thetas 100 times, as if each of these students took the test 100 times  
sim\_thetas\_n <- rep(sim\_thetas, each = 100)  
  
# Simulate the sum scores that these students received, using the item parameters for this test (assume these item parameters are estimated perfectly)  
sim\_sum\_scores <- rowSums(sim(my\_ip, sim\_thetas\_n))  
  
# Combine the thetas and sum scores into a data frame  
sim1\_long <- as.data.frame(cbind(sim\_thetas\_n, sim\_sum\_scores))  
  
# Rename column to the name expected by theta\_to\_scale\_score conversion  
colnames(sim1\_long) <- c("Theta", "sim\_sum\_scores")  
  
# Add column for scale scores (from thetas)  
sim1\_long$sim\_scale\_scores <- theta\_to\_scale\_score(sim1\_long$Theta)  
  
# Group the above data frame by sum scores, and summarize the different "true" thetas that could have produced each sum score  
sim1\_thetas <- sim1\_long %>%   
 group\_by(sim\_sum\_scores) %>%   
 summarise(tibble('2.5' = round(quantile(sim\_scale\_scores, 0.025), 0),  
 '10' = round(quantile(sim\_scale\_scores, 0.1), 0),  
 mean = round(mean(sim\_scale\_scores), 0),   
 median = round(median(sim\_scale\_scores), 0),   
 se = round(sd(sim\_scale\_scores), 1),  
 '90' = round(quantile(sim\_scale\_scores, 0.9), 0),  
 '97.5' = round(quantile(sim\_scale\_scores, 0.975), 0),   
 max = round(max(sim\_scale\_scores), 0),  
 nsims = n()))  
sim1\_thetas

## # A tibble: 31 x 10  
## sim\_sum\_scores `2.5` `10` mean median se `90` `97.5` max nsims  
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <int>  
## 1 1 105 105 105 105 NA 105 105 105 1  
## 2 2 89 92 103 100 12.9 118 139 139 30  
## 3 3 88 90 110 103 19.2 137 150 184 101  
## 4 4 88 92 111 106 19.1 138 157 182 329  
## 5 5 89 92 114 109 20.3 143 163 194 719  
## 6 6 88 92 117 111 23.5 149 178 228 1417  
## 7 7 89 92 121 117 25.4 157 183 222 2506  
## 8 8 89 94 126 121 27.5 166 189 221 3462  
## 9 9 90 96 133 129 29.7 174 197 253 4156  
## 10 10 91 99 141 139 32.4 185 208 267 4791  
## # … with 21 more rows

# Repeat the above, this time summarizing the different "true" scale scores that could have produced each sum score  
sim1\_scale\_scores <- sim1\_long %>%   
 group\_by(sim\_sum\_scores) %>%   
 summarise(tibble('2.5' = round(quantile(sim\_scale\_scores, 0.025), 0),  
 '10' = round(quantile(sim\_scale\_scores, 0.1), 0),  
 mean = round(mean(sim\_scale\_scores), 0),   
 median = round(median(sim\_scale\_scores), 0),   
 se = round(sd(sim\_scale\_scores), 1),  
 '90' = round(quantile(sim\_scale\_scores, 0.9), 0),  
 '97.5' = round(quantile(sim\_scale\_scores, 0.975), 0),   
 max = round(max(sim\_scale\_scores), 0),  
 nsims = n()))  
sim1\_scale\_scores

## # A tibble: 31 x 10  
## sim\_sum\_scores `2.5` `10` mean median se `90` `97.5` max nsims  
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <int>  
## 1 1 105 105 105 105 NA 105 105 105 1  
## 2 2 89 92 103 100 12.9 118 139 139 30  
## 3 3 88 90 110 103 19.2 137 150 184 101  
## 4 4 88 92 111 106 19.1 138 157 182 329  
## 5 5 89 92 114 109 20.3 143 163 194 719  
## 6 6 88 92 117 111 23.5 149 178 228 1417  
## 7 7 89 92 121 117 25.4 157 183 222 2506  
## 8 8 89 94 126 121 27.5 166 189 221 3462  
## 9 9 90 96 133 129 29.7 174 197 253 4156  
## 10 10 91 99 141 139 32.4 185 208 267 4791  
## # … with 21 more rows

# Can also create a histogram for the possible thetas that produced each sum score, for example:  
hist(sim1\_long$Theta[sim1\_long$sim\_sum\_scores == 20], freq = F)



# Appendix 2: Scale Score Estimation Using Full-Pattern Scoring

Full-pattern scoring (using a full table recording how each student performed on each question) can improve ability estimation.

# Use parameter estimates to simulate answers for 100 students  
# (Import student data here if using real answers)  
set.seed(88)  
sim\_thetas <- rnorm(1000)  
sim\_responses <- sim(my\_ip, sim\_thetas)  
  
# Put the parameter estimates and standard errors into the list structure that irtoys functions expect  
# Note: ability estimation function does not need standard errors or variance-covariance matrix to run  
parameter\_list <- list(est = my\_ip, se = NA, vcm = NA)  
  
# Estimate student thetas, based on full-pattern scoring, using MLE (several other methods exist for this "ability" function)  
mod\_MLE<- ability(resp = sim\_responses, ip = parameter\_list, method = "MLE")  
  
# Look at the first five rows  
mod\_MLE[1:5, ]

## est sem n  
## [1,] -1.1985497 1.0216098 31  
## [2,] 0.4882736 0.8668540 31  
## [3,] 2.9747950 1.0424542 31  
## [4,] -2.1205461 1.2139283 31  
## [5,] 0.5835620 0.8651891 31

# Convert these estimated thetas to scale scores and achievement levels  
ability\_df <- as.data.frame(mod\_MLE)  
colnames(ability\_df) <- c("Theta", "se(Theta)", "QuestionsAnswered")  
ability\_df$ScaleScore <- theta\_to\_scale\_score(ability\_df$Theta)  
ability\_df$AchievementLevel <- scale\_score\_to\_achievement\_level(ability\_df$ScaleScore)  
  
# Round the scale scores to 0 dp before reporting  
ability\_df$ScaleScore <- round(ability\_df$ScaleScore, 0)  
  
# View table:  
ability\_df

## Theta se(Theta) QuestionsAnswered ScaleScore AchievementLevel  
## 1 -1.198549721 1.0216098 31 205 Below Basic  
## 2 0.488273592 0.8668540 31 256 Proficient  
## 3 2.974794957 1.0424542 31 333 Advanced  
## 4 -2.120546071 1.2139283 31 176 Below Basic  
## 5 0.583561985 0.8651891 31 259 Proficient  
## 6 0.345894269 0.8706878 31 252 Proficient  
## 7 -0.233786359 0.9033941 31 234 Basic  
## 8 -3.999931695 1.8805408 31 119 Below Basic  
## 9 -1.365085407 1.0504287 31 200 Below Basic  
## 10 0.239805324 0.8746052 31 249 Basic  
## 11 -1.578158011 1.0910399 31 193 Below Basic  
## 12 2.346990431 0.9567203 31 314 Advanced  
## 13 1.808157751 0.9050213 31 297 Advanced  
## 14 -0.753307669 0.9568772 31 218 Basic  
## 15 0.791131314 0.8640252 31 266 Proficient  
## 16 -0.196600598 0.9004549 31 235 Basic  
## 17 1.635665341 0.8927793 31 292 Advanced  
## 18 1.697093620 0.8968969 31 294 Advanced  
## 19 -1.082020734 1.0029485 31 208 Below Basic  
## 20 1.896567224 0.9121108 31 300 Advanced  
## 21 -0.739271530 0.9551235 31 219 Basic  
## 22 -1.365710222 1.0505416 31 200 Below Basic  
## 23 0.349945854 0.8705562 31 252 Proficient  
## 24 -1.466929427 1.0693121 31 196 Below Basic  
## 25 0.424275451 0.8683766 31 255 Proficient  
## 26 -1.241706366 1.0288342 31 203 Below Basic  
## 27 0.418267288 0.8685364 31 254 Proficient  
## 28 -0.521145456 0.9300892 31 225 Basic  
## 29 -1.910636828 1.1629829 31 183 Below Basic  
## 30 -0.999830571 0.9905239 31 211 Below Basic  
## 31 -0.737928454 0.9549566 31 219 Basic  
## 32 1.536023877 0.8866726 31 289 Advanced  
## 33 1.031615325 0.8668194 31 273 Proficient  
## 34 0.009679705 0.8862644 31 242 Basic  
## 35 0.729741815 0.8640208 31 264 Proficient  
## 36 -1.757093352 1.1284430 31 187 Below Basic  
## 37 -2.077234742 1.2030598 31 178 Below Basic  
## 38 0.657791258 0.8643874 31 262 Proficient  
## 39 -2.412642286 1.2921690 31 167 Below Basic  
## 40 -3.999925722 1.8805380 31 119 Below Basic  
## 41 1.581776574 0.8893884 31 290 Advanced  
## 42 1.564930928 0.8883711 31 290 Advanced  
## 43 -0.208184722 0.9013580 31 235 Basic  
## 44 0.606297565 0.8648976 31 260 Proficient  
## 45 -2.687903925 1.3739830 31 159 Below Basic  
## 46 -0.666917534 0.9463583 31 221 Basic  
## 47 -0.725564890 0.9534278 31 219 Basic  
## 48 1.967282610 0.9181769 31 302 Advanced  
## 49 0.488729700 0.8668443 31 256 Proficient  
## 50 0.327556184 0.8712999 31 252 Proficient  
## 51 0.474317476 0.8671582 31 256 Proficient  
## 52 0.374732686 0.8697801 31 253 Proficient  
## 53 -3.016774649 1.4824131 31 149 Below Basic  
## 54 0.734725073 0.8640103 31 264 Proficient  
## 55 -0.124560024 0.8950931 31 238 Basic  
## 56 0.822850498 0.8641413 31 267 Proficient  
## 57 -0.312478771 0.9100014 31 232 Basic  
## 58 -0.124743925 0.8951063 31 238 Basic  
## 59 1.797907912 0.9042350 31 297 Advanced  
## 60 0.224607093 0.8752412 31 248 Basic  
## 61 1.174171120 0.8705329 31 278 Proficient  
## 62 -0.283438754 0.9075017 31 233 Basic  
## 63 1.292419862 0.8747559 31 281 Proficient  
## 64 1.655656636 0.8940898 31 292 Advanced  
## 65 -0.268751769 0.9062649 31 233 Basic  
## 66 -0.785942114 0.9610217 31 217 Basic  
## 67 0.812599053 0.8640954 31 266 Proficient  
## 68 0.659754614 0.8643720 31 262 Proficient  
## 69 1.823755771 0.9062321 31 298 Advanced  
## 70 -1.506668114 1.0769419 31 195 Below Basic  
## 71 0.983480115 0.8659091 31 272 Proficient  
## 72 -1.021834756 0.9937907 31 210 Below Basic  
## 73 2.632222033 0.9922681 31 322 Advanced  
## 74 1.505788331 0.8849603 31 288 Advanced  
## 75 -0.186092220 0.8996455 31 236 Basic  
## 76 2.209784147 0.9416342 31 309 Advanced  
## 77 1.753047876 0.9008809 31 295 Advanced  
## 78 -0.990964271 0.9892199 31 211 Below Basic  
## 79 1.204315917 0.8715116 31 278 Proficient  
## 80 -1.091020918 1.0043460 31 208 Below Basic  
## 81 0.585329734 0.8651650 31 259 Proficient  
## 82 -0.561673185 0.9344267 31 224 Basic  
## 83 0.295791145 0.8724243 31 251 Proficient  
## 84 0.426973383 0.8683058 31 255 Proficient  
## 85 -1.227447014 1.0264284 31 204 Below Basic  
## 86 0.119843845 0.8801392 31 245 Basic  
## 87 -0.964978640 0.9854385 31 212 Below Basic  
## 88 -1.777910298 1.1329926 31 187 Below Basic  
## 89 -0.487507015 0.9265972 31 226 Basic  
## 90 -0.229692969 0.9030648 31 234 Basic  
## 91 -0.892341259 0.9751887 31 214 Basic  
## 92 0.499837338 0.8666136 31 257 Proficient  
## 93 -1.435484433 1.0633790 31 197 Below Basic  
## 94 -1.662936714 1.1083824 31 190 Below Basic  
## 95 2.630054605 0.9919767 31 322 Advanced  
## 96 -0.199367278 0.9006695 31 235 Basic  
## 97 1.584278948 0.8895413 31 290 Advanced  
## 98 0.550081429 0.8656923 31 258 Proficient  
## 99 1.330889612 0.8763511 31 282 Advanced  
## 100 -0.476205433 0.9254460 31 227 Basic  
## 101 -0.176585984 0.8989213 31 236 Basic  
## 102 -1.886097662 1.1573095 31 184 Below Basic  
## 103 -2.599175041 1.3467367 31 162 Below Basic  
## 104 -3.999928759 1.8805394 31 119 Below Basic  
## 105 -0.744939668 0.9558296 31 219 Basic  
## 106 1.305829992 0.8752997 31 282 Proficient  
## 107 -2.328535698 1.2687486 31 170 Below Basic  
## 108 -0.498930657 0.9277721 31 226 Basic  
## 109 -1.711264866 1.1185733 31 189 Below Basic  
## 110 1.274755891 0.8740598 31 281 Proficient  
## 111 0.040564924 0.8844458 31 243 Basic  
## 112 -0.388167886 0.9168551 31 230 Basic  
## 113 0.756664924 0.8639869 31 265 Proficient  
## 114 0.668313777 0.8643086 31 262 Proficient  
## 115 2.187485846 0.9393062 31 309 Advanced  
## 116 -0.697558009 0.9500141 31 220 Basic  
## 117 0.154434963 0.8784225 31 246 Basic  
## 118 1.472923456 0.8831737 31 287 Advanced  
## 119 1.212852422 0.8718009 31 279 Proficient  
## 120 1.998976724 0.9210094 31 303 Advanced  
## 121 1.051679427 0.8672503 31 274 Proficient  
## 122 1.231130786 0.8724385 31 279 Proficient  
## 123 0.161397558 0.8780888 31 246 Basic  
## 124 -0.302465646 0.9091314 31 232 Basic  
## 125 0.144296306 0.8789154 31 246 Basic  
## 126 0.065933064 0.8830112 31 243 Basic  
## 127 0.129185001 0.8796659 31 245 Basic  
## 128 -0.025072637 0.8884056 31 241 Basic  
## 129 2.102307760 0.9307318 31 306 Advanced  
## 130 0.619096584 0.8647514 31 260 Proficient  
## 131 -2.860348737 1.4293609 31 154 Below Basic  
## 132 -2.220500408 1.2397274 31 173 Below Basic  
## 133 -0.782206467 0.9605426 31 217 Basic  
## 134 -1.135570301 1.0113712 31 207 Below Basic  
## 135 -0.973763755 0.9867101 31 212 Below Basic  
## 136 0.319968447 0.8715610 31 251 Proficient  
## 137 2.568464952 0.9838315 31 320 Advanced  
## 138 -1.649609542 1.1056111 31 191 Below Basic  
## 139 -2.392596541 1.2865208 31 168 Below Basic  
## 140 0.468938574 0.8672796 31 256 Proficient  
## 141 -3.999955515 1.8805519 31 119 Below Basic  
## 142 0.033372527 0.8848622 31 242 Basic  
## 143 -0.945288257 0.9826135 31 212 Below Basic  
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## 940 -0.527773368 0.9307888 31 225 Basic  
## 941 -0.832066601 0.9670399 31 216 Basic  
## 942 -1.333213065 1.0447162 31 201 Below Basic  
## 943 -0.322592413 0.9108888 31 232 Basic  
## 944 -1.967566066 1.1763710 31 181 Below Basic  
## 945 -1.901466921 1.1608560 31 183 Below Basic  
## 946 0.505926672 0.8664913 31 257 Proficient  
## 947 -2.764570699 1.3982053 31 157 Below Basic  
## 948 -1.872145961 1.1541100 31 184 Below Basic  
## 949 -0.301874036 0.9090802 31 232 Basic  
## 950 0.651494176 0.8644387 31 261 Proficient  
## 951 -1.345023867 1.0468221 31 200 Below Basic  
## 952 -1.047386666 0.9976388 31 209 Below Basic  
## 953 2.496511036 0.9746497 31 318 Advanced  
## 954 0.384743002 0.8694807 31 253 Proficient  
## 955 -0.619676740 0.9408830 31 222 Basic  
## 956 -0.761087405 0.9578567 31 218 Basic  
## 957 1.378982815 0.8784973 31 284 Advanced  
## 958 0.200331248 0.8762962 31 248 Basic  
## 959 1.147950191 0.8697363 31 277 Proficient  
## 960 1.646609161 0.8934932 31 292 Advanced  
## 961 -0.590623929 0.9376125 31 223 Basic  
## 962 -2.240278871 1.2449518 31 173 Below Basic  
## 963 -0.762091701 0.9579835 31 218 Basic  
## 964 0.397137488 0.8691210 31 254 Proficient  
## 965 -0.318213742 0.9105035 31 232 Basic  
## 966 -0.393883630 0.9173927 31 229 Basic  
## 967 -3.332797705 1.5979934 31 139 Below Basic  
## 968 -1.722186373 1.1209072 31 189 Below Basic  
## 969 -0.603236638 0.9390233 31 223 Basic  
## 970 1.562025407 0.8881976 31 289 Advanced  
## 971 1.276909166 0.8741434 31 281 Proficient  
## 972 1.094150183 0.8682618 31 275 Proficient  
## 973 0.799237623 0.8640476 31 266 Proficient  
## 974 -1.537087673 1.0828821 31 194 Below Basic  
## 975 -1.478601073 1.0715378 31 196 Below Basic  
## 976 -1.233753210 1.0274901 31 204 Below Basic  
## 977 -0.062789421 0.8908434 31 240 Basic  
## 978 -0.842661607 0.9684490 31 216 Basic  
## 979 -1.938839609 1.1695758 31 182 Below Basic  
## 980 -0.534940771 0.9315496 31 225 Basic  
## 981 0.499226644 0.8666260 31 257 Proficient  
## 982 0.145946125 0.8788346 31 246 Basic  
## 983 1.867817991 0.9097451 31 299 Advanced  
## 984 0.490415164 0.8668087 31 257 Proficient  
## 985 1.454142176 0.8821877 31 286 Advanced  
## 986 1.977339426 0.9190681 31 302 Advanced  
## 987 -0.333778421 0.9118805 31 231 Basic  
## 988 -0.203285753 0.9009747 31 235 Basic  
## 989 1.478221056 0.8834565 31 287 Advanced  
## 990 1.011881508 0.8664251 31 273 Proficient  
## 991 -0.069708603 0.8913035 31 239 Basic  
## 992 -0.837284431 0.9677326 31 216 Basic  
## 993 -0.080689725 0.8920420 31 239 Basic  
## 994 0.371362247 0.8698827 31 253 Proficient  
## 995 -1.585725004 1.0925603 31 193 Below Basic  
## 996 1.154658814 0.8699352 31 277 Proficient  
## 997 -0.124734399 0.8951056 31 238 Basic  
## 998 1.837513283 0.9073143 31 298 Advanced  
## 999 -0.905300516 0.9769829 31 214 Below Basic  
## 1000 -0.906135765 0.9770990 31 214 Below Basic

# Export the data   
write.csv(ability\_df, file = "Estimated\_Scores\_From\_Full\_Pattern\_Scores.csv", row.names = F)

# Appendix 3: Diagnostics

## Diagnostics and other test plots:

# Simulate data  
set.seed(88)  
sim\_thetas <- rnorm(1000)  
sim\_responses <- sim(my\_ip, sim\_thetas)  
  
# Classical Test Theory EDA metrics:  
# Note: Because the simulated data is pre-graded, we're saying the "answer key" is 1, 1, 1, 1, 1....  
ctt <- tia(sim\_responses, key = rep(1, 31))  
  
# Show Cronbach's alpha for this "test":  
ctt$testlevel$alpha

## [1] 0.5014108

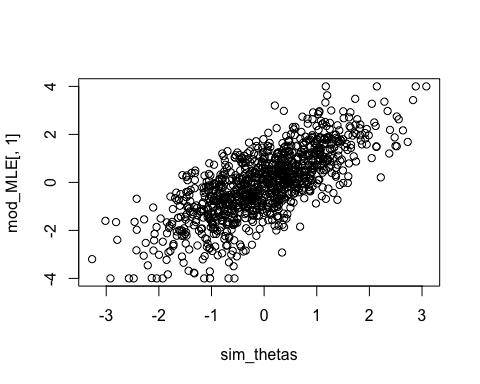
# Show CTT item-level statistics for first five items  
ctt$itemlevel[1:5, ]

## Prop. correct Item-sum cor. Alpha without  
## Item1 0.670 0.2060123 0.4808992  
## Item2 0.598 0.2845038 0.4677427  
## Item3 0.583 0.2972614 0.4654726  
## Item4 0.609 0.1781749 0.4846593  
## Item5 0.765 0.1851781 0.4851434

# Estimate student thetas, based on full-pattern scoring, using MLE (several other methods exist for this "ability" function)  
mod\_MLE<- ability(resp = sim\_responses, ip = parameter\_list, method = "MLE")  
  
# How does the MLE ability estimation perform compared to the "true thetas" from our simulation?  
cor(mod\_MLE[,1], sim\_thetas)

## [1] 0.7368264

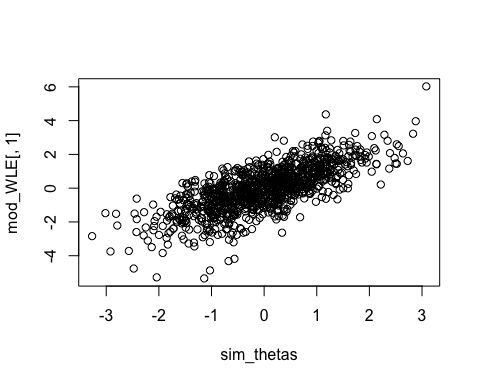
plot(sim\_thetas, mod\_MLE[,1])



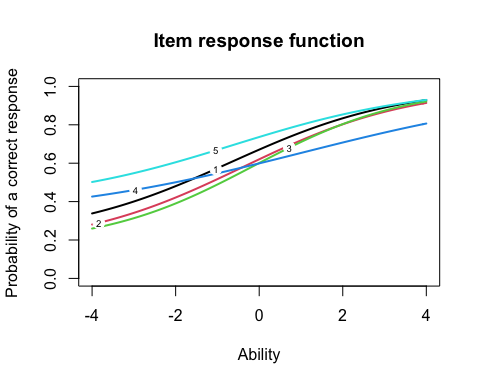
# How do other ability estimation methods perform?  
mod\_WLE <- ability(resp = sim\_responses, ip = parameter\_list, method = "WLE")  
cor(mod\_WLE[,1], sim\_thetas)

## [1] 0.7336838

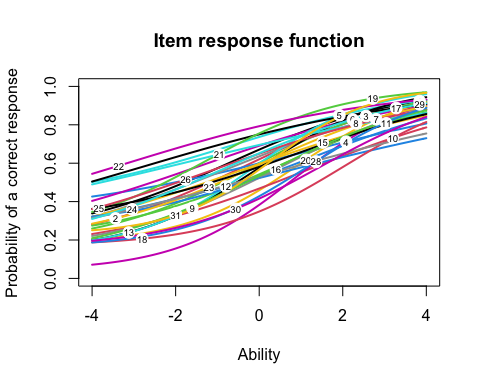
plot(sim\_thetas, mod\_WLE[,1])



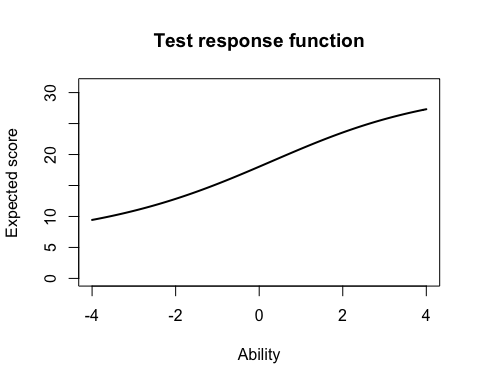
# Item Characteristic Curves for first five items (this package calls them "item response functions")  
plot(irf(my\_ip, items = 1:5), co = NA, label = T)



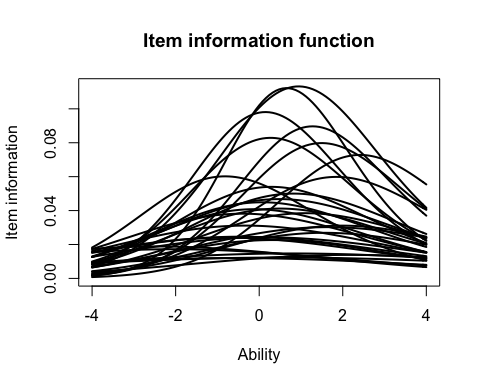
# ICCs for all items:  
plot(irf(my\_ip), co = NA, label = T)



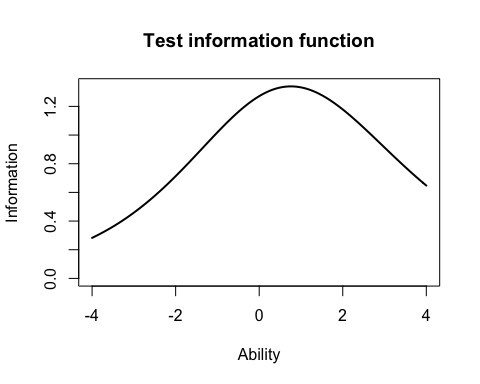
# Test Characteristic Curve (this package calls this a "test response function")  
plot(trf(my\_ip))



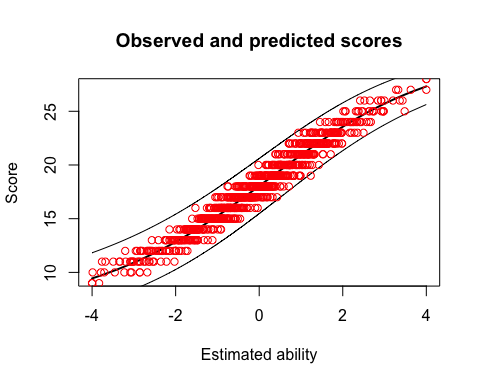
# Overlaid item information curves  
plot(iif(my\_ip))



# Test information function  
plot(tif(my\_ip))



# Cool plot of observed sum scores and predicted sum scores against estimated ability, with +/- 1se bands  
scp(sim\_responses, my\_ip)



# "Empirical response function" for a selected item: observed sum scores vs. percent correct on this question  
item\_1\_erf <- erf(sim\_responses, 1)

